

# OPTIMIZANDO ACORDES EN LA MÚSICA POPULAR



Víctor Pérez García  
victperez@uv.mx

Universidad Veracruzana, México

18 de noviembre de 2016

victacordes D.R. ©

**Con la frente marchita  
(Joaquín Sabina)**

Gm7 Cm7 F7 Bb7Maj Eb7Maj  
Sentados en corro merendábamos besos y porros  
Am7(b5) D7 Gm7  
y las horas pasaban de prisa entre el humo y la risa  
F  
te morías por volver  
Ab Gm7 F Eb  
con la frente marchita cantaba Gardel  
Cm7 D7 Gm7  
y entre citas de Borges Evita bailaba con Freud  
Cm7 Am7(b5) D7 Gm7  
ya llovió desde aquel chaparrón hasta hoy

Bb F  
Iba cada domingo a tu puesto del rastro a comprarte  
Ab Bb Eb  
carricoches de miga de pan soldaditos de lata  
Bb F  
con agüita del mar Andaluz quise yo enamorarte  
Ab Bb Eb  
pero tú no querías más amor que el del Río de la Plata

Cm7 F7 Bb7Maj Eb7Maj  
Duró la tormenta hasta entrados los años ochenta  
Am7(b5) D7 Gm7  
luego el sol fue secando la ropa de la vieja Europa  
F  
no hay nostalgia peor,  
Ab Gm7 F Eb  
que añorar lo que nunca jamás sucedió  
Cm7 D7 Gm7  
mándame una postal de San Telmo, adiós, cuidate  
Cm7 Am7(b5) D7 Gm7  
y sonó entre tú y yo el silbato del tren

Bb F  
Iba cada domingo a tu puesto del rastro a comprarte  
Ab Bb Eb  
monigotes de miga de pan caballitos de lata  
Bb F  
con agüita del mar Andaluz quise yo enamorarte  
Ab Bb Eb  
pero tú no tenías otro amor que el del Río de la Plata

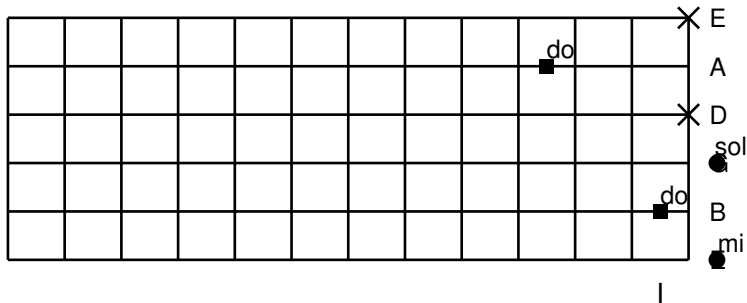
Gm7 Am7(b5) D7  
Gm7 Am7(b5) D7

Cm7 F7 Bb7Maj Eb7Maj  
Aqueellas banderas de la patria de la primavera  
Am7(b5) D7 Gm7  
a decirme que existe el olvido, esta noche han venido  
F  
te sentaba tan bien  
Ab Gm7 F Eb  
esa boina calada al estilo del Che  
Cm7 D7 Gm7  
Buenos Aires es como contabas hoy fui a pasear  
Cm7 Am7(b5) D7 Gm7  
y al llegar a la Plaza de Mayo me dio,  
Cm7 Am7(b5) D7 Gm7  
por llorar y me puse a gritar ¿dónde estás?

Bb F  
Y no volví más, a tu puesto del rastro a comprarte  
Ab Bb Eb  
corazones de miga de pan, sombreritos de lata  
Bb F  
y ya nadie me escribe diciendo no consigo olvidarte  
Ab Bb Eb  
ojalá que estuvieras conmigo en el Río de la Plata  
Bb F  
y no volví más, a tu puesto del rastro a comprarte  
Ab Bb Eb  
carricoches de miga de pan soldaditos de lata

Gm7 Am7(b5) D7  
Gm7 Am7(b5) D7 Gm7

Notación y terminología: Trastes (trabajaremos del 0 al 11).  
do mayor



Se representa por x3x010.  
Usaremos acordes con 4 voces

## CLASES DE ACORDES QUE USAREMOS

*C, Cm, Cm7, Cm7Maj, Cm2, Cm6, Cm9,  
C6, C9, C9b, C(69), C7(b5), C7(#5), C7(b9),  
C7(9), C7(#9), C7(69), C7(6#9), C7(#11), C7sus4, Csus4,  
Csus2, C7Maj9, C + 7, C+, Cm7(b5), Cdis, C7Maj, C7.*

Y acordes con bajo:

*C/F, Cm/F, Cm7/F, C7/F.*

Un total de 29 calidades de acordes diferentes, además cuatro de ellos incluyen bajo adicional. Se considera un total de 396 acordes distintos. Usar hasta tres trastes consecutivos.

Del traste 0 al 11 hay 3030 formas distintas de digitar estos acordes.

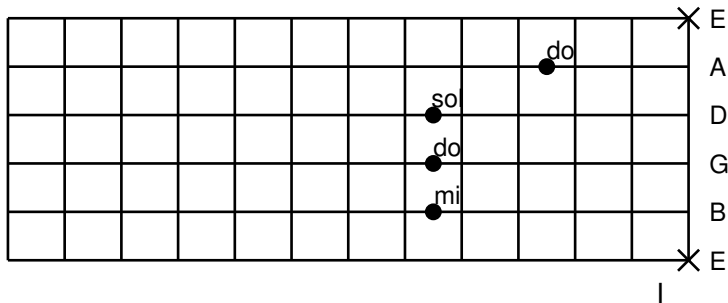
Dado el conjunto de digitaciones  $\mathcal{D}$  definimos una métrica  $d : \mathcal{D} \times \mathcal{D}$  con las siguientes propiedades:

- Si entre el acorde  $c_1$  y el acorde  $c_2$  solo hay un cambio de un dedo, un traste, la distancia será  $d(c_1, c_2) = 1$ .
- Subir o bajar un dedo un traste cuesta a lo más 2.
- El diámetro se alcanza en los acordes  $0000xx$  y  $xx12.12.12.12$ .
- Si nos restringimos a los trastes  $t_1 < t_2$ , el diámetro se alcanza en los acordes  $t_1 t_1 t_1 t_1 xx$  y  $xx t_2 t_2 t_2 t_2$ .

Obtenemos un espacio métrico en  $\mathcal{D}$  que mide el esfuerzo de pasar de un acorde a otro.

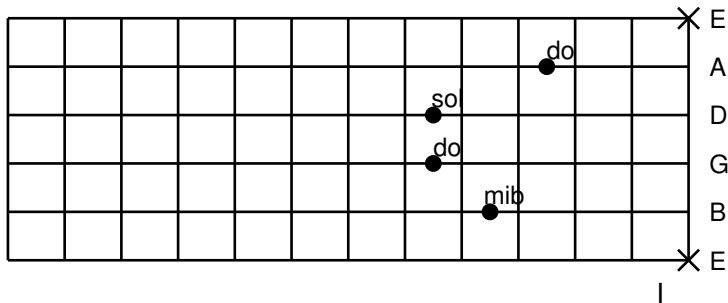
$$d(x3555x, x3554x) = 1.$$

do mayor a do menor



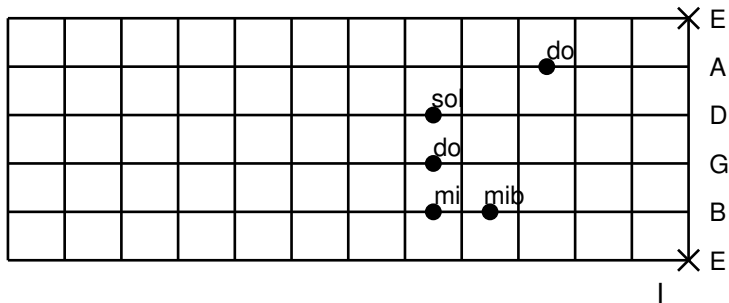
$$d(x3555x, x3554x) = 1.$$

do mayor a do menor



$$d(x3555x, x3554x) = 1.$$

do mayor a do menor





## UNA CANCIÓN COMO PRODUCTO CARTESIANO

Una canción se puede ver como un producto cartesiano de digitaciones de acordes:

$$S = \mathcal{A}_1 \times \mathcal{A}_2 \times \dots \times \mathcal{A}_n,$$

donde cada elemento de  $S$  es una forma de tocar una secuencia de acordes dada por la canción.

Por ejemplo, nuestra canción se puede ver:

$$S = Gm7 \times Cm7 \times \dots \times Gm7,$$

donde  $Gm7$  son las formas distintas de digitar sol menor con séptima en la guitarra, etc.

La secuencia de 110 acordes de la canción es la siguiente:

*Gm7, Cm7, F7, Bb7M, Eb7M, Am7(b5), D7, Gm7, F, Ab, Gm7, F, Eb, Cm7, D7, Gm7, Cm7, Am7(b5), D7, Gm7, Bb, F, Ab, Bb, Eb, Bb, F, Ab, Bb, Eb, Cm7, F7, Bb7M, Eb7M, Am7(b5), D7, Gm7, F, Ab, Gm7, F, Eb, Cm7, D7, Gm7, Cm7, Am7(b5), D7, Gm7, Bb, F, Ab, Bb, Eb, Bb, F, Ab, Bb, Eb, Gm7, Am7(b5), D7, Gm7, Am7(b5), D7, Cm7, F7, Bb7M, Eb7M, Am7(b5), D7, Gm7, F, Ab, Gm7, F, Eb, Cm7, D7, Gm7, Cm7, Am7(b5), D7, Gm7, Cm7, Am7(b5), D7, Gm7, Bb, F, Ab, Bb, Eb, Bb, F, Ab, Bb, Eb, Bb, F, Ab, Bb, Eb, Gm7, Am7(b5), D7, Gm7, Am7(b5), D7, Gm7.*



Vamos a medir la dificultad de tocar cada una de estas versiones.  
Dado  $v = a_1 \times a_2 \times \cdots \times a_n \in \mathcal{S}$ , definimos su peso como

$$w(v) = d(a_1, a_2) + d(a_2, a_3) + \cdots + d(a_{n-1}, a_n).$$

El objetivo es hallar la canción de peso mínimo:

$$\min_{v \in \mathcal{S}} w(v).$$

Dado los número grandes, usamos programación dinámica para resolver el problema.



# SOLUCIÓN, 0-11, FUNDAMENTAL

Gm7 [-1, 10, 8, 10, 8, -1]  
Cm7 [8, -1, 8, 8, 8, -1]  
F7 [-1, 8, 7, 8, 6, -1]  
Bb7M [6, -1, 7, 7, 6, -1]  
Eb7M [-1, 6, 8, 7, 8, -1]  
Am7(b5) [5, -1, 5, 5, 4, -1]  
D7 [-1, 5, 4, 5, 3, -1]  
Gm7 [3, -1, 3, 3, 3, -1]  
F [1, -1, 3, 2, 1, -1]  
G# [4, -1, 6, 5, 4, -1]  
Gm7 [3, -1, 3, 3, 3, -1]  
F [1, -1, 3, 2, 1, -1]  
Eb [-1, 6, -1, 0, 4, 6]  
Cm7 [-1, 3, 5, 3, 4, -1]  
D7 [-1, 5, 4, 5, 3, -1]  
Gm7 [3, -1, 3, 3, 3, -1]  
Cm7 [-1, 3, 5, 3, 4, -1]  
Am7(b5) [5, -1, 5, 5, 4, -1]  
D7 [-1, 5, 4, 5, 3, -1]  
Gm7 [3, -1, 3, 3, 3, -1]  
Bb [-1, 1, 3, 3, 3, -1]  
F [1, -1, 3, 2, 1, -1]  
G# [4, -1, 6, 5, 4, -1]  
Bb [-1, 1, 3, 3, 3, -1]  
Eb [-1, 6, -1, 0, 4, 6]  
Bb [-1, 1, 3, 3, 3, -1]  
F [1, -1, 3, 2, 1, -1]  
G# [4, -1, 6, 5, 4, -1]  
Bb [-1, 1, 3, 3, 3, -1]  
Cm7 [8, -1, 8, 8, 8, -1]  
F7 [-1, 8, 7, 8, 6, -1]  
Bb7M [6, -1, 7, 7, 6, -1]  
Eb7M [-1, 6, 8, 7, 8, -1]  
Am7(b5) [5, -1, 5, 5, 4, -1]  
D7 [-1, 5, 4, 5, 3, -1]  
Gm7 [3, -1, 3, 3, 3, -1]

F [1, -1, 3, 2, 1, -1]  
G# [4, -1, 6, 5, 4, -1]  
Gm7 [3, -1, 3, 3, 3, -1]  
F [1, -1, 3, 2, 1, -1]  
Eb [-1, 6, -1, 0, 4, 6]  
Cm7 [-1, 3, 5, 3, 4, -1]  
D7 [-1, 5, 4, 5, 3, -1]  
Gm7 [3, -1, 3, 3, 3, -1]  
Cm7 [-1, 3, 5, 3, 4, -1]  
Am7(b5) [5, -1, 5, 5, 4, -1]  
D7 [-1, 5, 4, 5, 3, -1]  
Gm7 [3, -1, 3, 3, 3, -1]  
Bb [-1, 1, 3, 3, 3, -1]  
F [1, -1, 3, 2, 1, -1]  
G# [4, -1, 6, 5, 4, -1]  
Bb [-1, 1, 3, 3, 3, -1]  
Eb [-1, 6, -1, 0, 4, 6]  
Bb [-1, 1, -1, 3, 3, 1]  
F [1, -1, -1, 2, 1, 1]  
G# [4, -1, -1, 5, 4, 4]  
Bb [6, -1, -1, 7, 6, 6]  
Eb [-1, 6, -1, 8, 8, 6]  
Gm7 [-1, -1, 5, 7, 6, 6]  
Am7(b5) [5, -1, 5, 5, 4, -1]  
D7 [-1, 5, 4, 5, 3, -1]  
Gm7 [3, -1, 3, 3, 3, -1]  
Am7(b5) [5, -1, 5, 5, 4, -1]  
D7 [-1, 5, 4, 5, 3, -1]  
Cm7 [-1, 3, 1, 3, 1, -1]  
F7 [1, -1, 1, 2, 1, -1]  
Bb7M [-1, 1, 3, 2, 3, -1]  
Eb7M [-1, -1, 1, 3, 3, 3]  
Am7(b5) [-1, 0, -1, 5, 4, 3]  
D7 [-1, 5, 4, 5, 3, -1]  
Gm7 [3, -1, 3, 3, 3, -1]  
F [1, -1, 3, 2, 1, -1]  
G# [4, -1, 6, 5, 4, -1]

Gm7 [3, -1, 3, 3, 3, -1]  
F [1, -1, 3, 2, 1, -1]  
Eb [-1, 6, -1, 0, 4, 6]  
Cm7 [-1, 3, 5, 3, 4, -1]  
D7 [-1, 5, 4, 5, 3, -1]  
Gm7 [3, -1, 3, 3, 3, -1]  
Cm7 [-1, 3, 5, 3, 4, -1]  
Am7(b5) [5, -1, 5, 5, 4, -1]  
D7 [-1, 5, 4, 5, 3, -1]  
Gm7 [3, -1, 3, 3, 3, -1]  
Cm7 [-1, 3, 5, 3, 4, -1]  
Am7(b5) [5, -1, 5, 5, 4, -1]  
D7 [-1, 5, 4, 5, 3, -1]  
Gm7 [3, -1, 3, 3, 3, -1]  
Bb [-1, 1, 3, 3, 3, -1]  
F [1, -1, 3, 2, 1, -1]  
G# [4, -1, 6, 5, 4, -1]  
Bb [-1, 1, 3, 3, 3, -1]  
Eb [-1, 6, -1, 0, 4, 6]  
Bb [-1, 1, -1, 3, 3, 1]  
F [1, -1, -1, 2, 1, 1]  
G# [4, -1, -1, 5, 4, 4]  
Bb [6, -1, -1, 7, 6, 6]  
Eb [-1, 6, -1, 0, 4, 6]  
Bb [-1, 1, -1, 3, 3, 1]  
F [1, -1, -1, 2, 1, 1]  
G# [4, -1, -1, 5, 4, 4]  
Bb [6, -1, -1, 7, 6, 6]  
Eb [-1, 6, -1, 8, 8, 6]  
Gm7 [-1, -1, 5, 7, 6, 6]  
Am7(b5) [5, -1, 5, 5, 4, -1]  
D7 [-1, 5, 4, 5, 3, -1]  
Gm7 [3, -1, 3, 3, 3, -1]  
Am7(b5) [5, -1, 5, 5, 4, -1]  
D7 [-1, 5, 4, 5, 3, -1]  
Gm7 [3, -1, 3, 3, 3, -1]

$$S = Gm7 \times Cm7 \times \dots \times Gm7.$$

Hay

20065154331998078689488112002152218876  
04938267624393508489218171392396180442  
025843357770771228262400000000000

$$\approx 2 \times 10^{109}$$

acordes con inversiones.

# SOLUCIÓN, 0-11, INVERSIONES

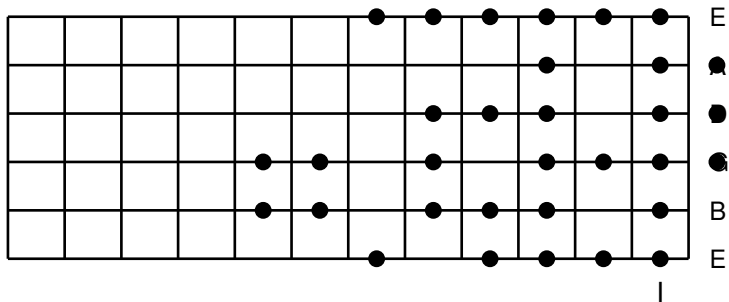
Gm7 [3, -1, 3, 3, 3, -1]  
Cm7 [-1, 3, 5, 3, 4, -1]  
F7 [-1, 3, 3, 2, 4, -1]  
Bb7M [-1, 1, 3, 2, 3, -1]  
Eb7M [-1, 1, 1, 0, 3, -1]  
Am7(b5) [-1, 0, 1, 0, 1, -1]  
D7 [2, -1, 0, 2, 1, -1]  
Gm7 [-1, 1, 3, 0, 3, -1]  
F [-1, 0, 3, 2, 1, -1]  
G# [-1, 3, 1, 1, 1, -1]  
Gm7 [-1, 1, 3, 0, 3, -1]  
F [-1, 3, 3, 2, 1, -1]  
Eb [3, -1, -1, 3, 4, 3]  
Cm7 [-1, 3, -1, 3, 4, 3]  
D7 [-1, 0, 4, 5, 3, -1]  
Gm7 [3, -1, 3, 3, 3, -1]  
Cm7 [-1, 3, 5, 3, 4, -1]  
Am7(b5) [-1, 0, 5, 5, 4, -1]  
D7 [-1, 0, 4, 5, 3, -1]  
Gm7 [3, -1, 3, 3, 3, -1]  
Bb [-1, 1, 3, 3, 3, -1]  
F [-1, 0, 3, 2, 1, -1]  
G# [-1, 3, 1, 1, 1, -1]  
Bb [1, -1, -1, 3, 3, 1]  
Eb [3, -1, -1, 3, 4, 3]  
Bb [1, -1, -1, 3, 3, 1]  
F [1, -1, 3, 2, 1, -1]  
G# [-1, 3, 1, 1, 1, -1]  
Bb [1, -1, -1, 3, 3, 1]  
Eb [3, -1, -1, 3, 4, 3]  
Cm7 [-1, 3, -1, 3, 4, 3]  
F7 [-1, 3, 3, 2, 4, -1]  
Bb7M [-1, 1, 3, 2, 3, -1]  
Eb7M [-1, 1, 1, 0, 3, -1]  
Am7(b5) [-1, 0, 1, 0, 1, -1]  
D7 [2, -1, 0, 2, 1, -1]  
Gm7 [-1, 1, 3, 0, 3, -1]

F [-1, 0, 3, 2, 1, -1]  
G# [-1, 3, 1, 1, 1, -1]  
Gm7 [-1, 1, 3, 0, 3, -1]  
F [-1, 3, 3, 2, 1, -1]  
Eb [3, -1, -1, 3, 4, 3]  
Cm7 [-1, -1, 1, 3, 1, 3]  
D7 [-1, -1, 0, 2, 1, 2]  
Gm7 [-1, 1, -1, 0, 3, 1]  
Cm7 [-1, -1, 1, 3, 1, 3]  
Am7(b5) [-1, -1, 1, 2, 1, 3]  
D7 [-1, -1, 0, 2, 1, 2]  
Gm7 [-1, 1, -1, 0, 3, 1]  
Bb [-1, 1, -1, 3, 3, 1]  
F [-1, 3, -1, 2, 1, 1]  
G# [4, -1, -1, 5, 4, 4]  
Bb [6, -1, -1, 7, 6, 6]  
Eb [6, -1, -1, 8, 8, 6]  
Bb [6, -1, -1, 7, 6, 6]  
F [5, -1, -1, 5, 6, 5]  
G# [4, -1, -1, 5, 4, 4]  
Bb [6, -1, -1, 7, 6, 6]  
Eb [6, -1, -1, 8, 8, 6]  
Gm7 [6, -1, 5, 7, 6, -1]  
Am7(b5) [5, -1, 5, 5, 4, -1]  
D7 [5, -1, 4, 5, 3, -1]  
Gm7 [3, -1, 3, 3, 3, -1]  
Am7(b5) [-1, 0, 5, 5, 4, -1]  
D7 [-1, 0, 4, 5, 3, -1]  
Cm7 [-1, 3, 5, 3, 4, -1]  
F7 [-1, 3, 3, 2, 4, -1]  
Bb7M [-1, 1, 3, 2, 3, -1]  
Eb7M [-1, 1, 1, 0, 3, -1]  
Am7(b5) [-1, 0, 1, 0, 1, -1]  
D7 [2, -1, 0, 2, 1, -1]  
Gm7 [-1, 1, 3, 0, 3, -1]  
F [-1, 0, 3, 2, 1, -1]  
G# [-1, 3, 1, 1, 1, -1]

Gm7 [-1, 1, 3, 0, 3, -1]  
F [-1, 3, 3, 2, 1, -1]  
Eb [3, -1, -1, 3, 4, 3]  
Cm7 [-1, -1, 1, 3, 1, 3]  
D7 [-1, -1, 0, 2, 1, 2]  
Gm7 [-1, 1, -1, 0, 3, 1]  
Cm7 [-1, -1, 1, 3, 1, 3]  
Am7(b5) [-1, -1, 1, 2, 1, 3]  
D7 [-1, -1, 0, 2, 1, 2]  
Gm7 [-1, 1, -1, 0, 3, 1]  
Cm7 [-1, -1, 1, 3, 1, 3]  
Am7(b5) [-1, -1, 1, 2, 1, 3]  
D7 [-1, -1, 0, 2, 1, 2]  
Gm7 [-1, 1, -1, 0, 3, 1]  
Cm7 [-1, -1, 1, 3, 1, 3]  
Am7(b5) [-1, -1, 1, 2, 1, 3]  
D7 [-1, -1, 0, 2, 1, 2]  
Gm7 [-1, 1, -1, 0, 3, 1]  
Bb [-1, 1, -1, 3, 3, 1]  
F [-1, 3, -1, 2, 1, 1]  
G# [4, -1, -1, 5, 4, 4]  
Bb [6, -1, -1, 7, 6, 6]  
Eb [6, -1, -1, 8, 8, 6]  
Bb [6, -1, -1, 7, 6, 6]  
F [5, -1, -1, 5, 6, 5]  
G# [4, -1, -1, 5, 4, 4]  
Bb [6, -1, -1, 7, 6, 6]  
Eb [6, -1, -1, 8, 8, 6]  
Bb [6, -1, -1, 7, 6, 6]  
F [5, -1, -1, 5, 6, 5]  
G# [4, -1, -1, 5, 4, 4]  
Bb [6, -1, -1, 7, 6, 6]  
Eb [6, -1, -1, 8, 8, 6]  
Bb [6, -1, -1, 7, 6, 6]  
F [5, -1, -1, 5, 6, 5]  
G# [4, -1, -1, 5, 4, 4]  
Bb [1, -1, -1, 3, 3, 1]  
Eb [3, -1, -1, 3, 4, 3]  
Gm7 [3, -1, -1, 3, 3, 1]  
Am7(b5) [-1, -1, 1, 2, 1, 3]  
D7 [-1, -1, 0, 2, 1, 2]  
Gm7 [-1, 1, -1, 0, 3, 1]  
Am7(b5) [-1, -1, 1, 2, 1, 3]  
D7 [-1, -1, 0, 2, 1, 2]  
Gm7 [-1, 1, -1, 0, 3, 1]



trastes usados



$$S = Gm7 \times Cm7 \times \dots \times Gm7.$$

Hay

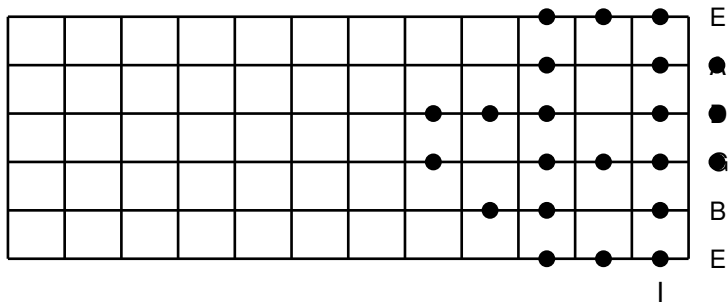
53707624969951797854963635085269132687  
5855997727782427688960000000000

$$\approx 5 \times 10^{68},$$

acordes con inversiones, del traste 0 al 5.



primeros trastes



*Gracias*