



Center for Research in Entertainment and Learning



# Discrete Musical Systems

Shlomo Dubnov



CELFI Seminar, Lecture 2



# Style Modeling and Machine Improvisation

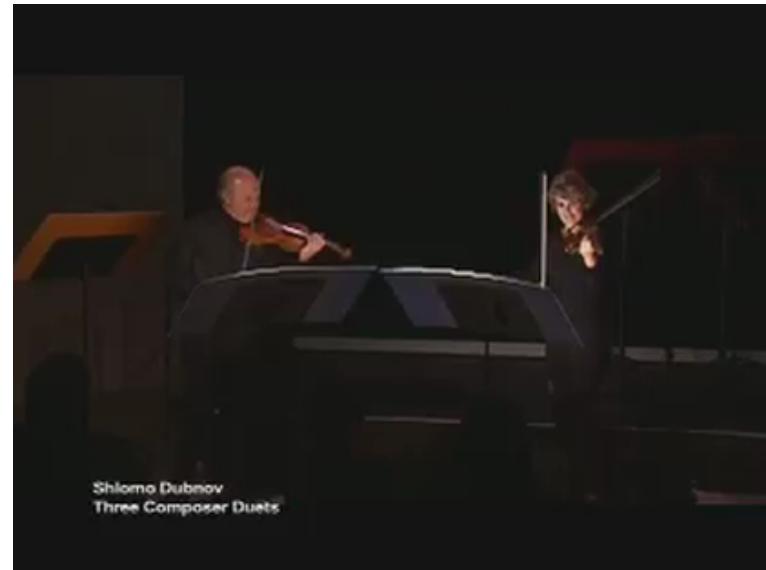
Machine learning of Variable Memory  
Markov models with focus on  
generative and interactive applications

# Machine Improvisation

PyOracle



Memex: Composer Duos



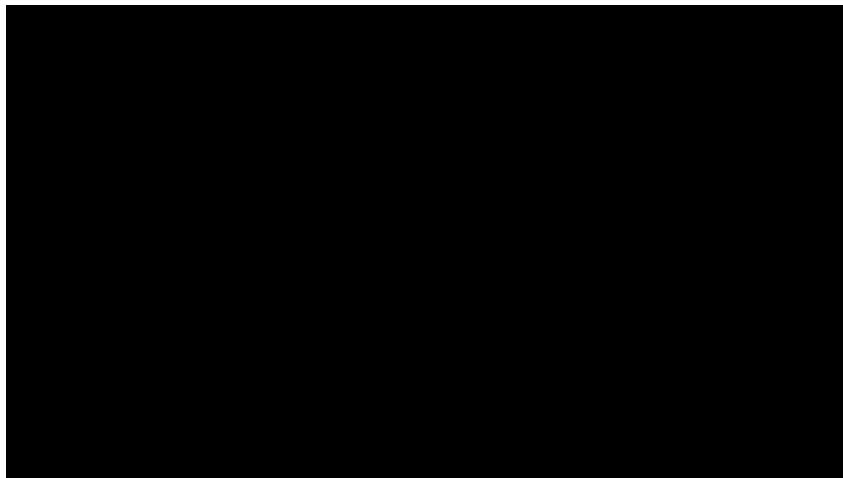
OMax



ircam  
Centre  
Pompidou

# Existing Systems

- Mimi
- Continuator
- Omax
- PyOracle
- ImroteK



# First paper on Machine Improvisation

## **Guessing the Composer's Mind: Applying Universal Prediction to Musical Style**

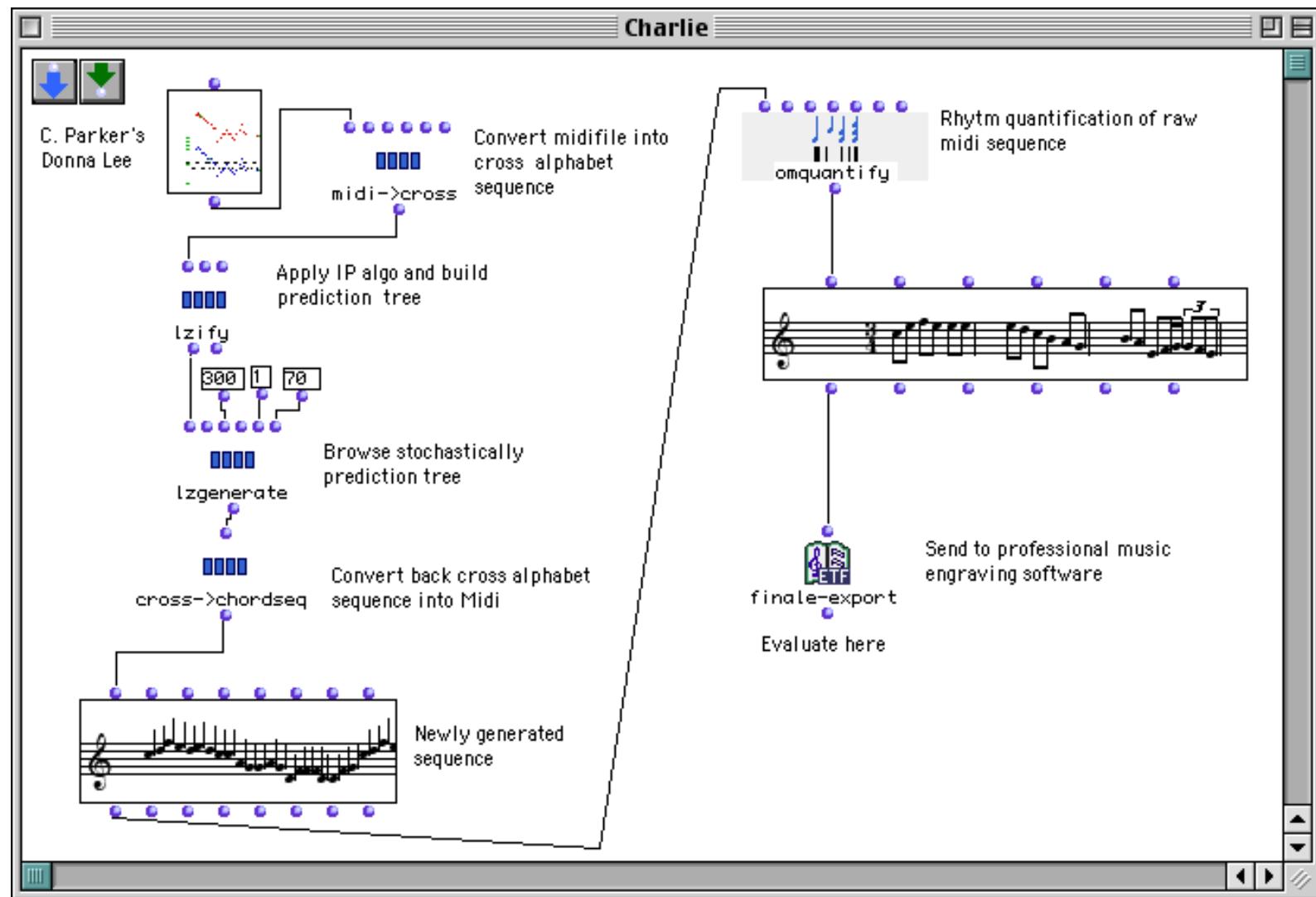
Gérard Assayag (Ircam) , Shlomo Dubnov (Ben Gurion Univ.), Olivier Delerue (Ircam)

### *Abstract*

In this paper, we present a dictionary based universal prediction algorithm that provides a very general and flexible approach to machine learning in the domain of musical style. Such operations as improvisation or assistance to composition can be realized on the resulting representations.

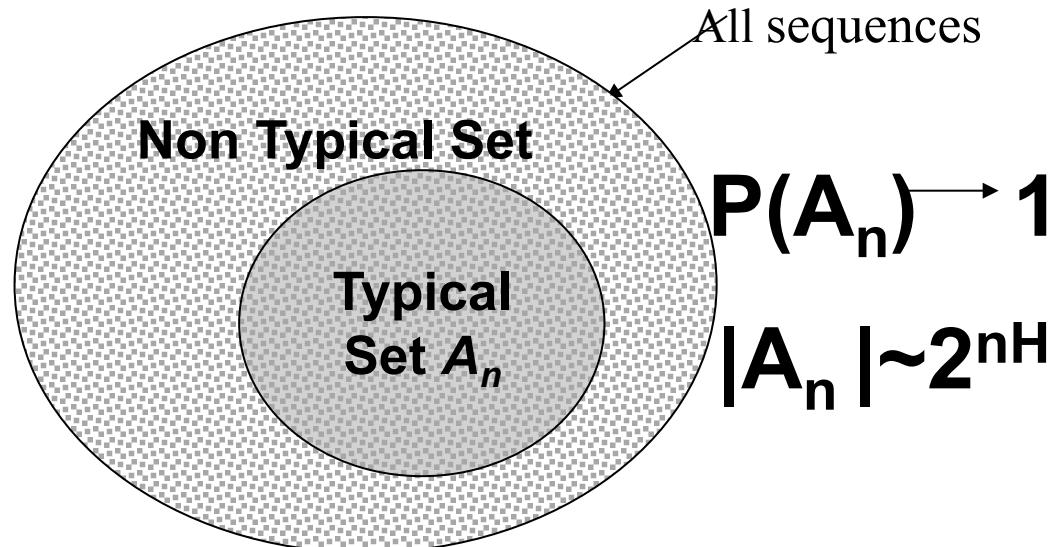
ICMC 1999

# Izify



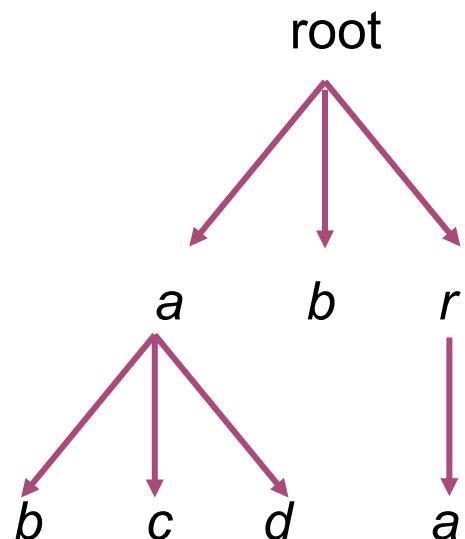
# Style Learning Algorithms

- Create Musical Generators from Examples that maintain *similarity* with the *style* of the original example



# Suffix Automata using LZ

- Analysis of “*abracadabra*”.



context : “”  
continuations :  $a$  (4/7),  $b$  (1/7),  $r$  (2/7).

context : “ $a$ ”  
continuations :  $b$  (1/3),  
 $c$  (1/3),  $d$  (1/3).

context : “ $r$ ”  
continuation :  $a$  (1/1).

$$P(\text{generate "abrac"}) = P(a|“”)P(b|\underline{a})P(r|ab)P(a|\underline{ab}\underline{r})P(c|\underline{abra}\underline{a}) = 4/7 \cdot 1/3 \cdot 2/7 \cdot 1 \cdot 1/3.$$

# IPMotif

```
def IPMotif(text):
    """Compute an associative dictionary (the motif dictionary)."""

    dictionary = {}
    motif = ""
    result = []
    for c in text:
        motif = motif + c
        if motif in dictionary:
            # Increase count for existing motif
#             print '%s in dictionary' % motif
            dictionary[motif] += 1
        else:
            # Add motif to the dictionary.
            dictionary[motif] = 1
            motif = ""
#             print 'add %s to dictionary' % motif

    return dictionary
```

```
{'a': 4, 'ac': 1, 'b': 1, 'ad': 1, 'r': 2, 'ra': 1, 'ab': 1}
```

# IPContinuation

```
def IPContinuation(dict1):
    """Compute continuation dictionary from a motif dictionary"""

    dict2 = {}
    for Wk in dict1:
        counter = dict1[Wk]
        W = Wk[:-1]
        k = Wk[-1]
        if W in dict2:
            dict2[W].append((k,counter))
        else:
            dict2[W] = [(k,counter)]
    dict2 = Normalize(dict2)
    return dict2

def Normalize(dict2):
    """Turns the counters in every element of dict2 to probabilities

    for W in dict2:
        cnt = [tup[1] for tup in dict2[W]]
        ttl = sum(cnt)
        for k,tup in enumerate(dict2[W]):
            dict2[W][k] = (tup[0],float(tup[1])/ttl)
    return dict2
```

```
{"": [('a', 0.57), ('b', 0.14), ('r', 0.28)], 'a': [('c', 0.33), ('d', 0.33), ('b', 0.33)], 'r': [('a', 1.0)]}
```

# Markov

```
def Markov(text,order=0):
    """Compute a Markov models (fixed length motif dictionary)."""

    dict3 = {}
    for i in range(len(text)-order):
        W = text[i:i+order]
        k = text[i+order]
        if W in dict3:
            if k in list(zip(*dict3[W])[0]):
                dict3[W][k] += 1
            else:
                dict3[W][k] = 1
        else:
            dict3[W] = {k:1}

    for x in dict3:
        dict3[x] = dict3[x].items()
    dict3 = Normalize(dict3)
    return dict3
```

```
{'a': [('c', 0.25), ('b', 0.5), ('d', 0.25)], 'r': [('a', 1.0)], 'b': [('r', 1.0)],
 'c': [('a', 1.0)], 'd': [('a', 1.0)]}
```

# Factor Oracle

- Extension of a Suffix tree
- Automaton that accepts all factors (substrings) of a string
- Effective language is larger then the set of factors and is hard to characterize
- Auxiliary construction points to suffixes for each point along the sequence
- We use the suffixes for improvisation

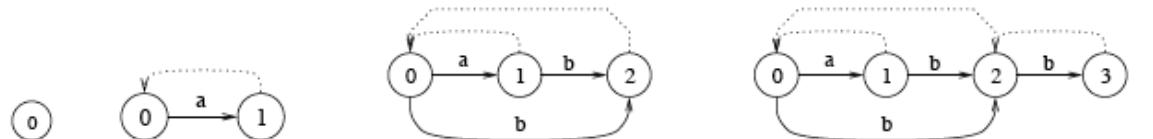
## Factor Oracle

$s = \text{"abbaab"}$

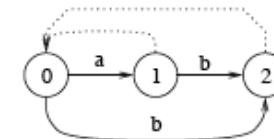
$[\text{trn}, \text{sfx}] = \text{FO}(s, a)$

```
% Factor Oracle for sequence s
% input:
% s - string of numbers in range [1,a]
% a - size of the alphabet
% output:
% trn - transition matrix (forward)
% sfx - suffix vector (backward)
```

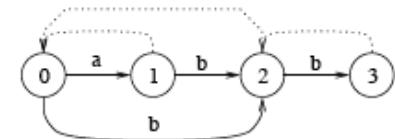
```
[s, kend, ktrace] = F0gen(trn,sfx,n,p,k)
% Generate new sequence using a Factor Oracle
% input:
% trn - transition table
% sfx - suffix vector
% n - length of new string
% p - probability of change
% k - starting point
% output:
% s - new sequence
% kend - end point
```



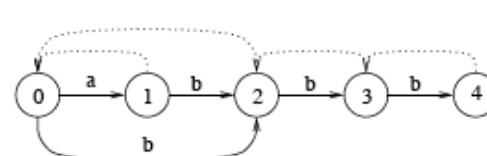
(a) Add  $a$



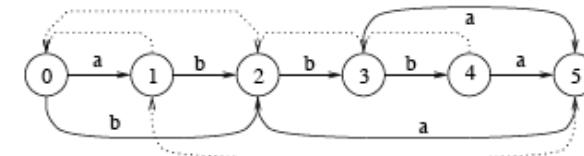
(c) Add  $b$



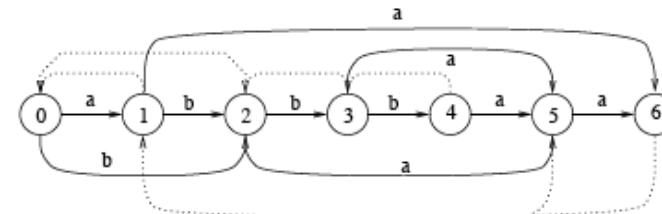
(d) Add  $b$



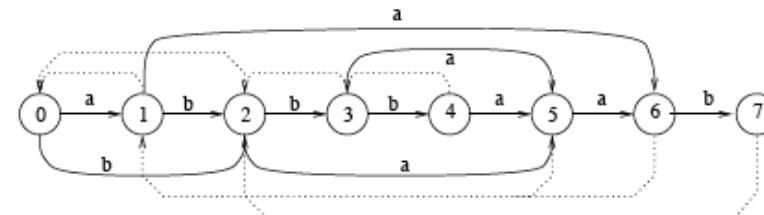
(e) Add  $b$



(f) Add  $a$



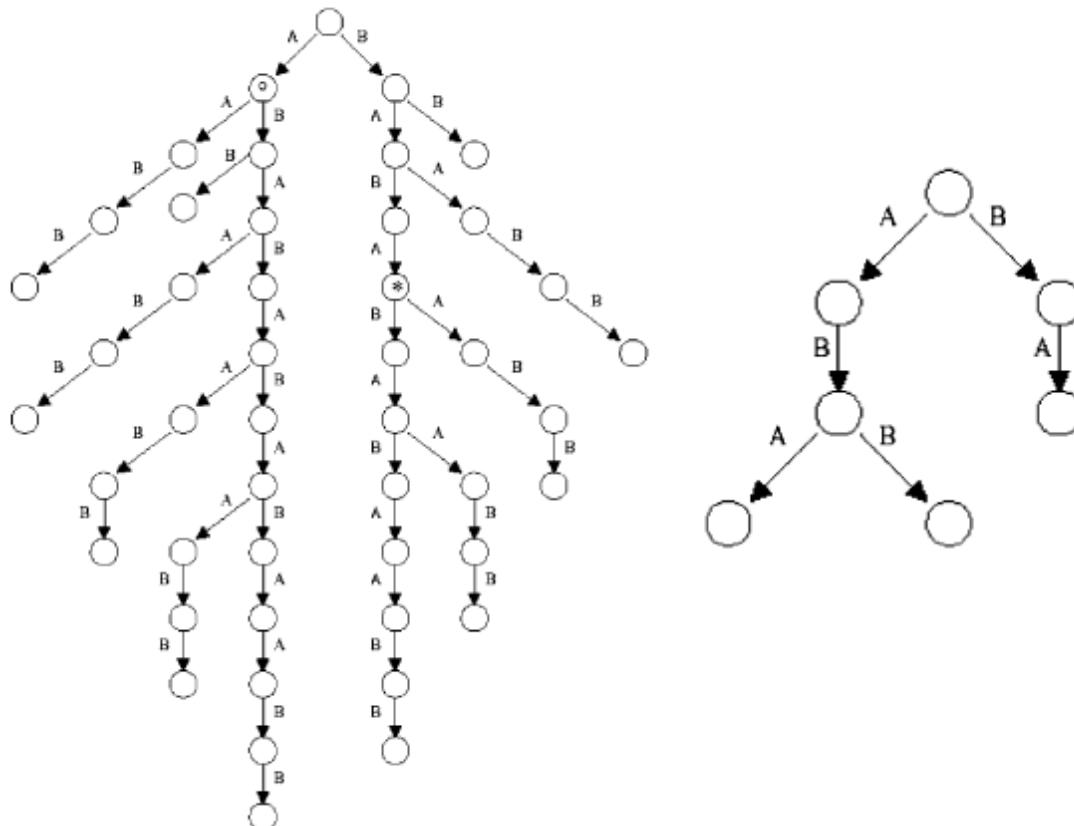
(g) Add  $a$



(h) Add  $b$

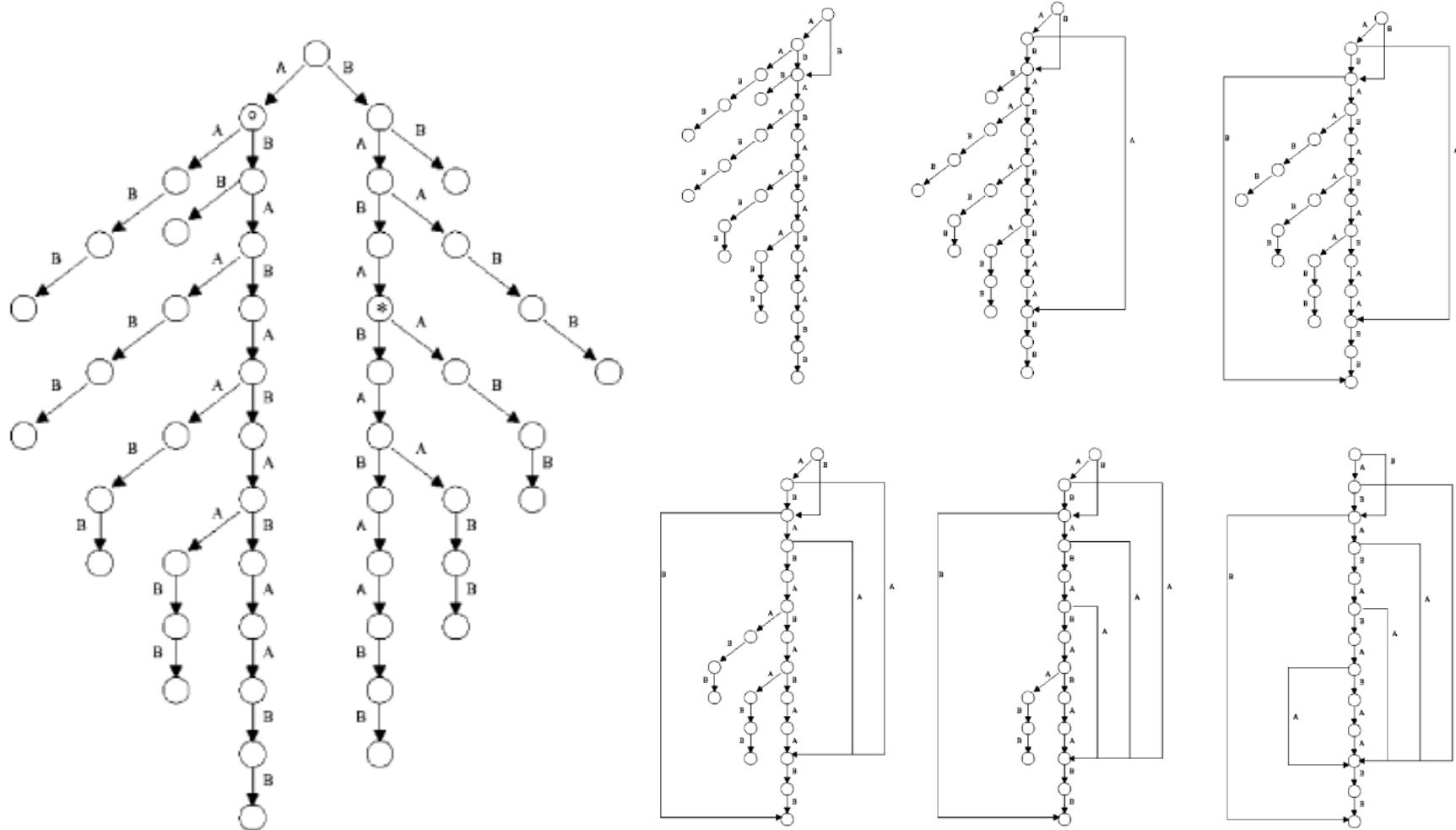
# Suffix Tree versus IP

$W = ABABABABAABB$

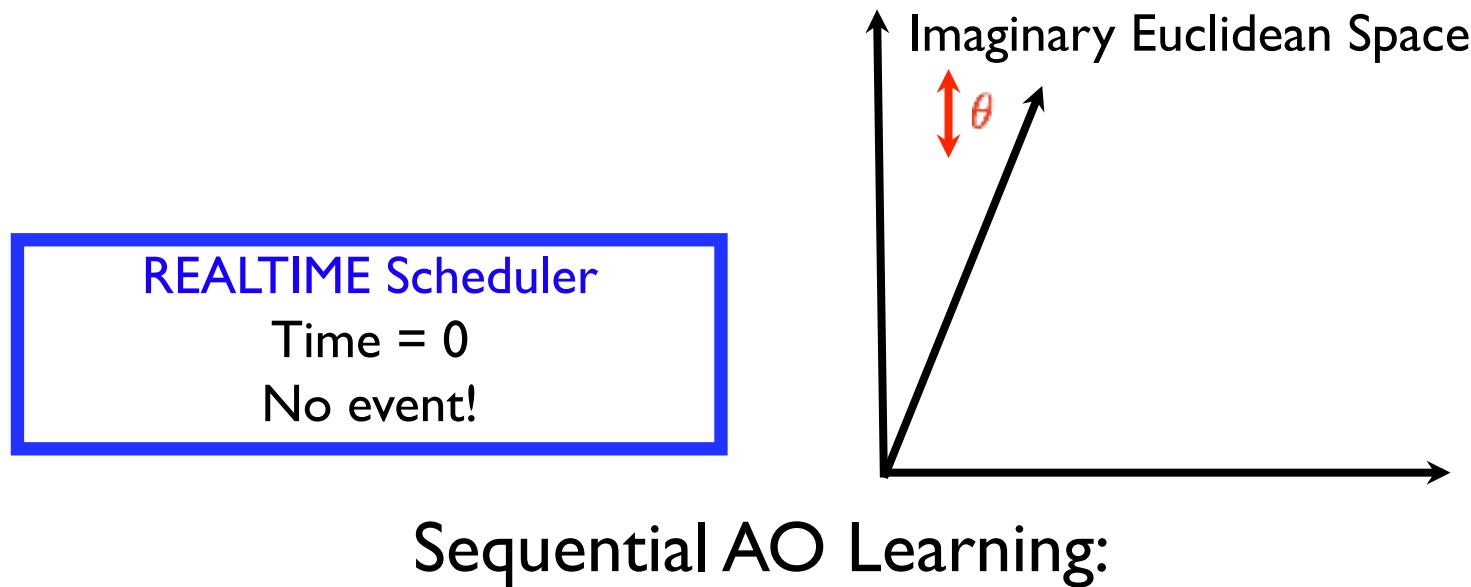


# From Suffix Tree to Factor Oracle

abababababaabb



# FO versus Audio Oracle Learning

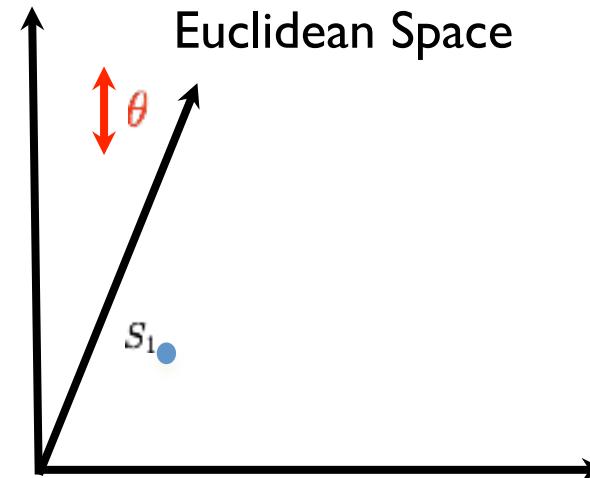


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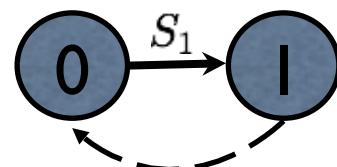
# FO versus Audio Oracle Learning

Create suffix link 1

REALTIME Scheduler  
Time = I  
Arrival of  $S_1$



Sequential AO Learning:



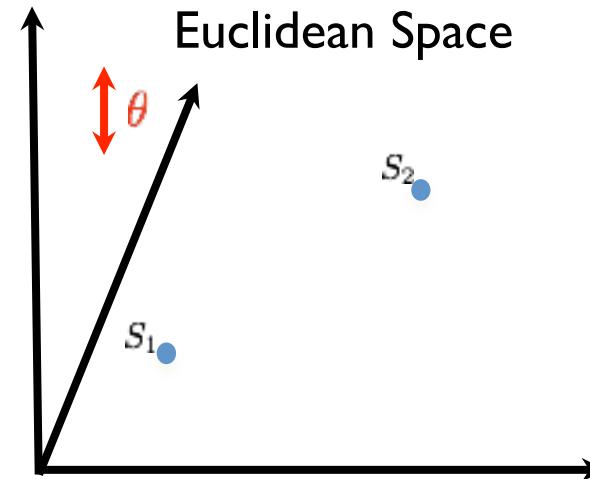
# FO versus Audio Oracle Learning

Follow suffix 1

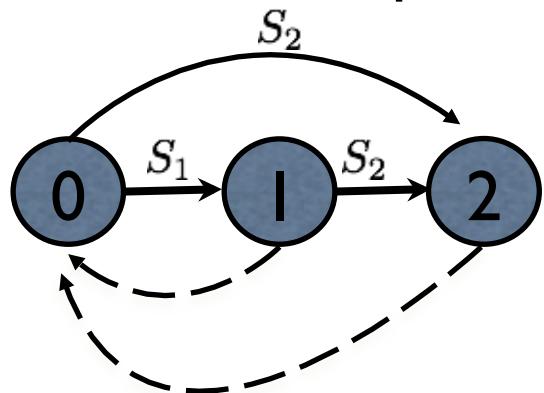
Create suffix 2

Create forward link 2

**REALTIME Scheduler**  
Time = 2  
Arrival of  $S_2$



## Sequential AO Learning:



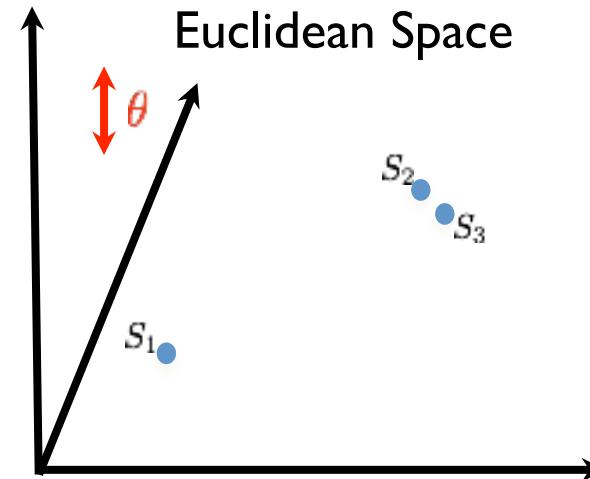
# FO versus Audio Oracle Learning

Follow suffix 2

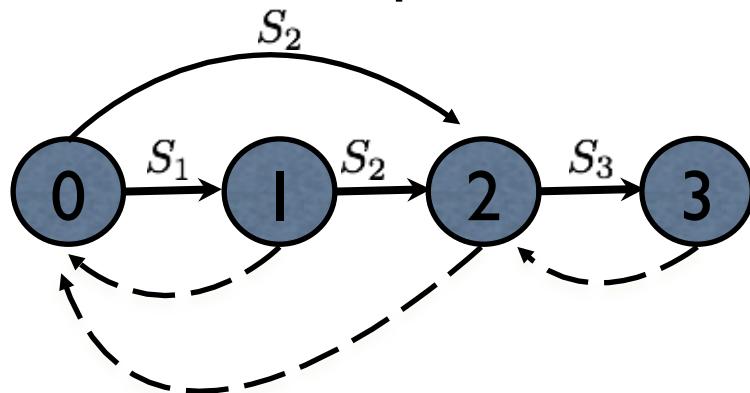
Follow forward link 2

Create suffix 3

**REALTIME Scheduler**  
Time = 3  
Arrival of  $S_3$



## Sequential AO Learning:



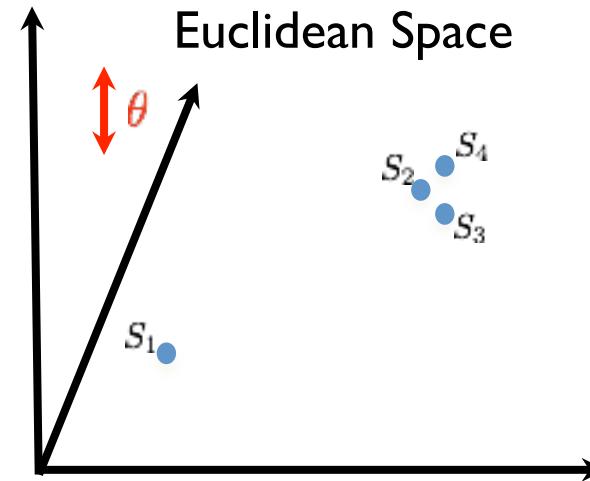
# FO versus Audio Oracle Learning

Follow suffix 3

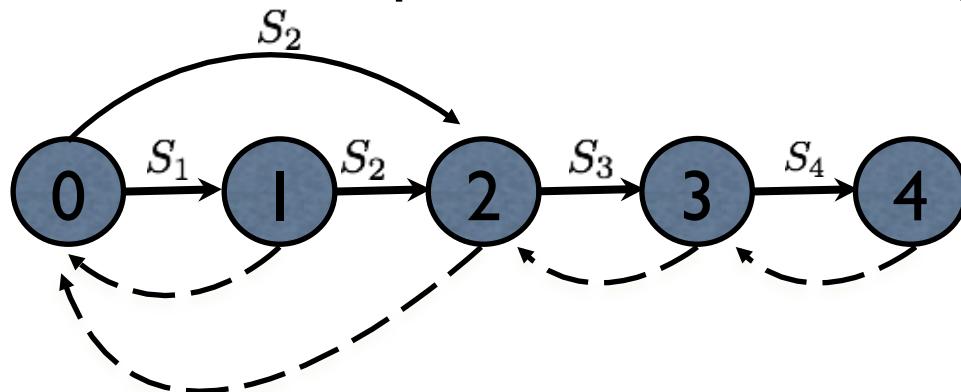
Follow forward link 3

Create suffix 4

**REALTIME Scheduler**  
Time = 4  
Arrival of  $S_4$

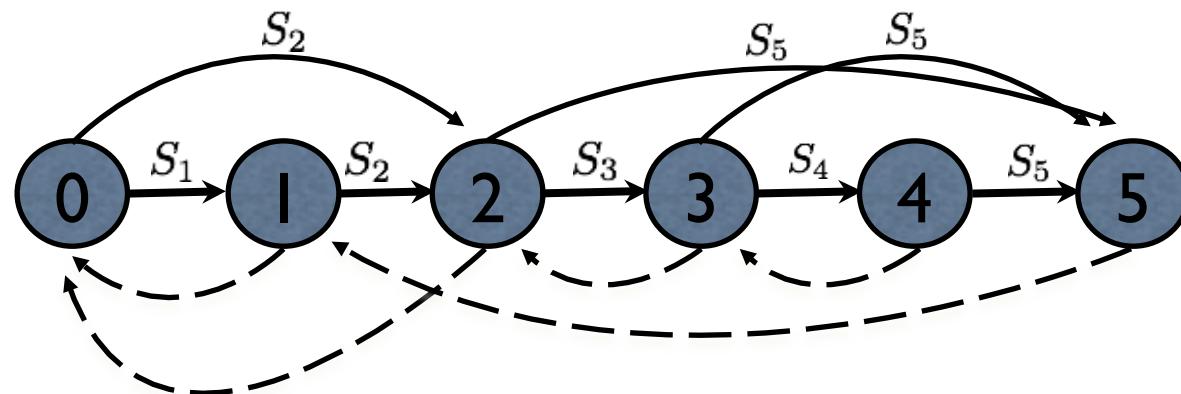
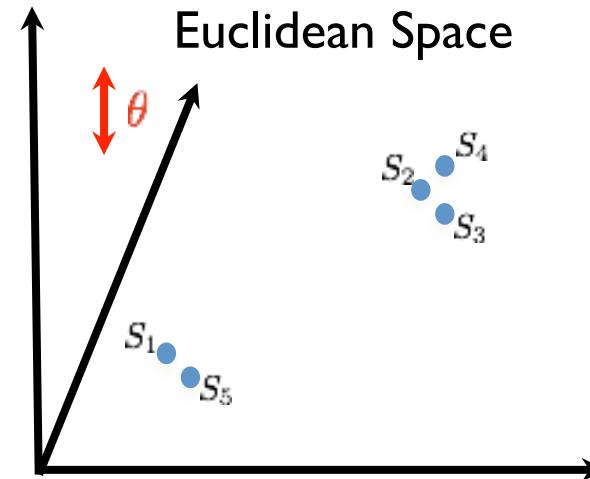


## Sequential AO Learning:



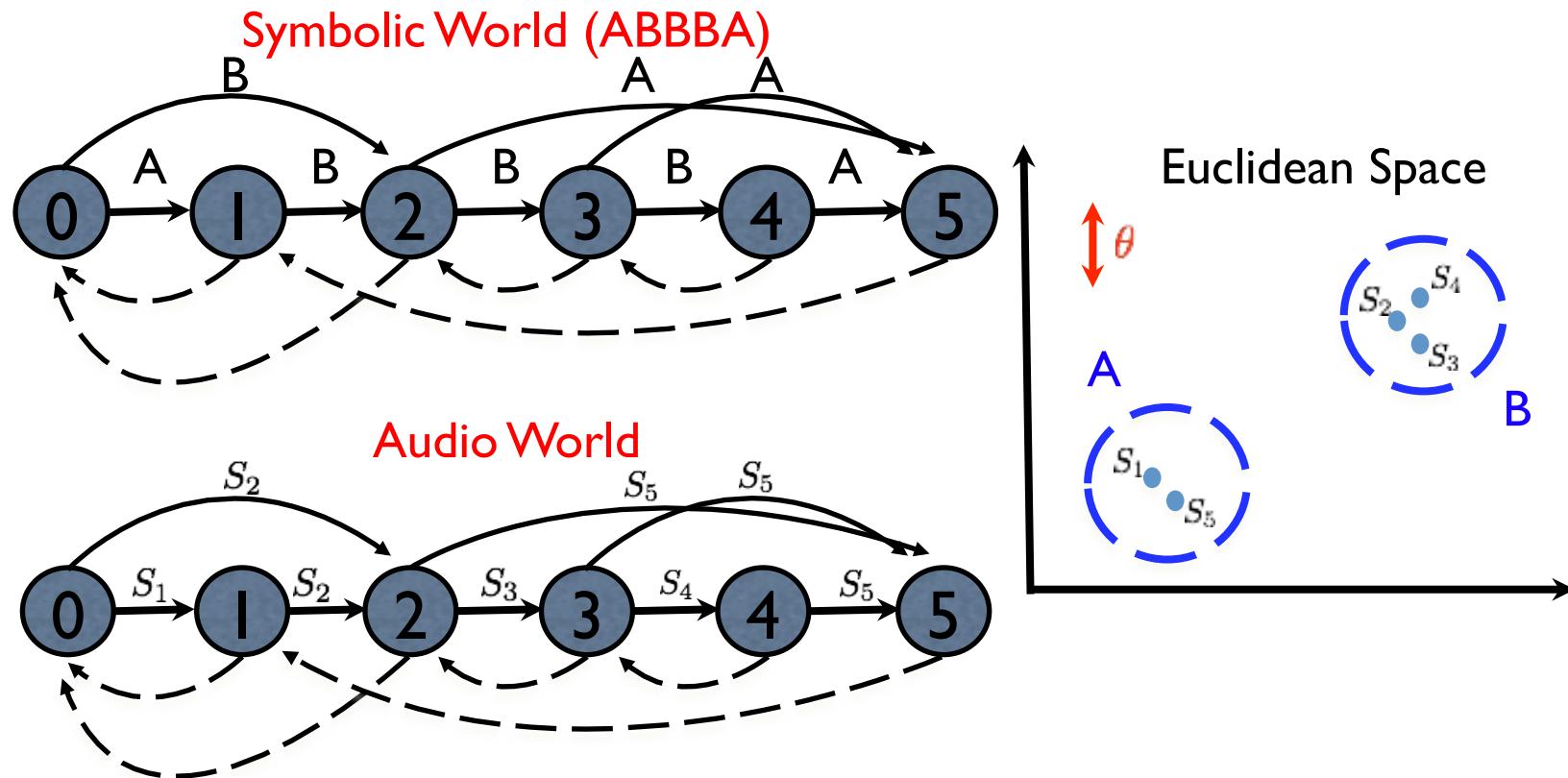
# FO versus Audio Oracle Learning

Follow suffix 4  
Create forward link 5  
Follow suffix 3  
Create forward link 5  
Follow suffix 2  
Follow forward link 1  
Create suffix 5

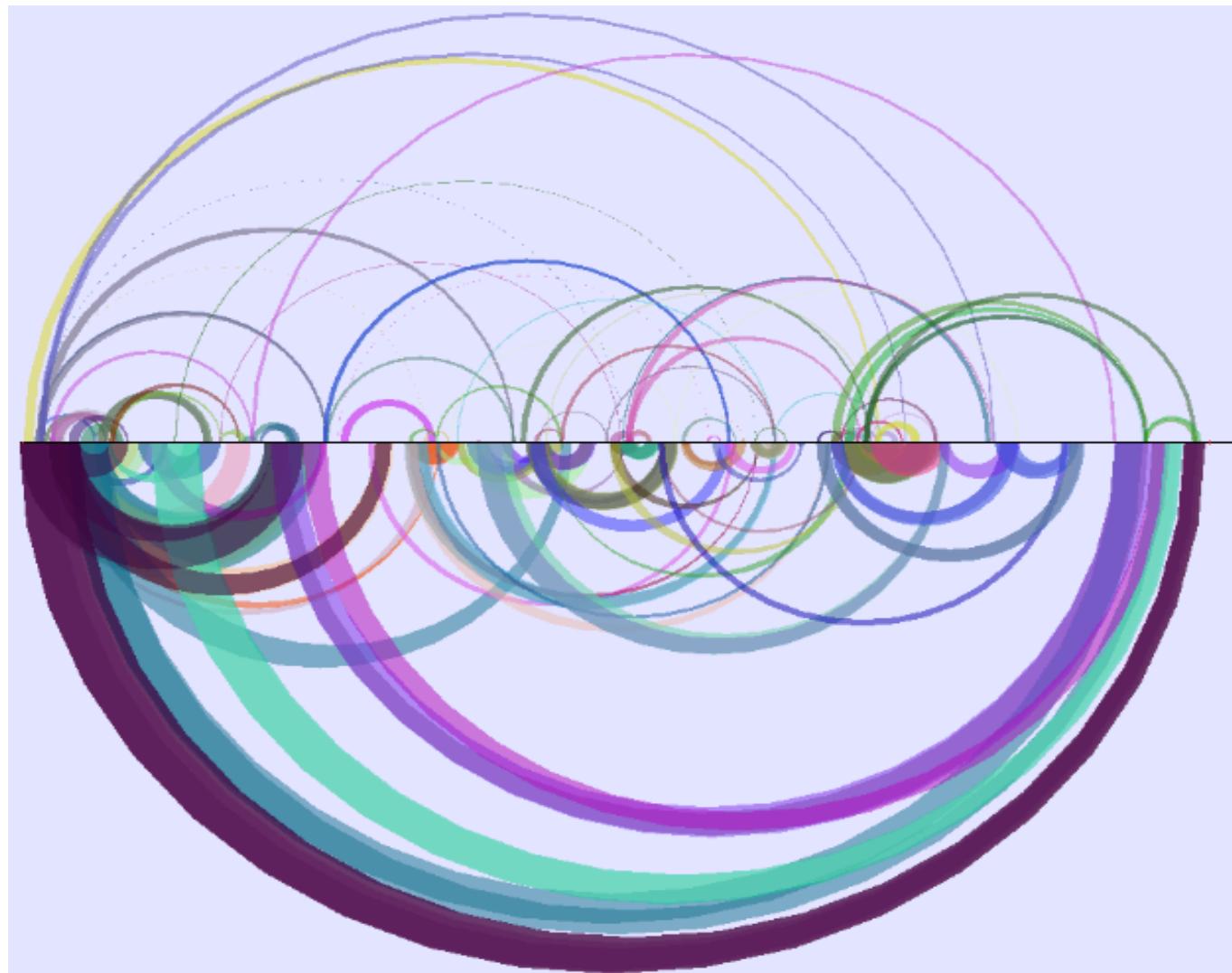


# Implicit Quantization

AO requires a threshold for symbolization / quantization



# Memory Trails





INTERNATIONAL COMPUTER MUSIC ASSOCIATION

## Guessing the Composer's Mind: Applying Universal Prediction to Musical Style

Assayag, Gérard; Dubnov, Shlomo; Delerue, Olivier, ICMC 1999

RESEARCH FEATURE

### Using Machine-Learning Methods for Musical Style Modeling

Research using statistical and information theoretic tools provides inference and prediction models that, to a certain extent, can generate new musical works imitating the style of the great masters.



Shlomo Dubnov, Gerard Assayag, Olivier Lartillot, Gill Bejerano, IEEE Computer, 2003, Issue 10

Using Factor Oracle for Machine Improvisation, G. Assayag and S. Dubnov, Soft Computing 8 (9), 2004



# Summary

- In LZify we are traversing the LZ tree using the longest suffix
- FO algorithm creates a “memory trail” in the form of suffix links pointing to longest repeated suffix (LRS)
- Suffix links and reverse suffix links constitute all points in a sequence that share a common history
- We can use these suffixes to “remix” the signal, i.e. “improvise”
- If we know how to measure similarity between signals, it is possible to generalize FO to Audio Oracle (FO over a metric space).

# Challenges

- What if the radius of the balls is unknown?
  - Using FO on an Audio Signal requires symbolization / quantization prior to FO
- Audio Signal Can be analyzed in terms of multiple features.
  - Which feature to choose?
- Specifying User Interaction and Musical Form

**Next: Information Dynamics criteria for symbolization using FO model**