

ON THE SIZE OF THE SOLUTIONS OF SPARSE POLYNOMIAL SYSTEMS

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We present sharp estimates for the size of the solution set of a sparse polynomial system, both in the function field and in the arithmetic settings. The obtained estimates make appear a new combinatorial invariant, the *mixed integral* of a family of concave functions. These results can be seen as analogues of the Bernstein-Kushnirenko theorem for rings of dimension 1.