Lower bounds in some problems of real Schubert calculus

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We single out some problems of Schubert calculus of subspaces of codimension 2 that have the property that all their solutions are real whenever the data are real. For other similar problems we prove non-trivial lower bounds for the number of real solutions. Our arguments explore the connection between subspaces of codimension 2 and rational functions of one variable.